

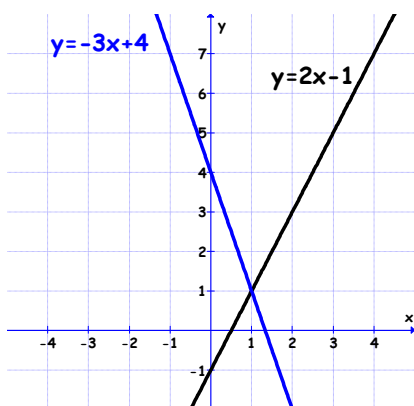
1. Solve by graphing:  $\begin{cases} y = 2x - 1 \\ y = -3x + 4 \end{cases}$

**Solution:**

To solve by graphing we need to graph both lines and look for the point of intersection they have:

$x$	$y = 2x - 1$
-1	$2(-1) - 1 = -3$
0	$2(0) - 1 = -1$
1	$2(1) - 1 = 1$

$x$	$y = -3x + 4$
0	$-3(0) + 4 = 4$
1	$-3(1) + 4 = 1$
2	$-3(2) + 4 = -2$



The point of intersection is (1, 1), so is the solution.

(1, 1)

2. Solve by substitution:  $\begin{cases} 2x + y = 4 \\ 3x - 2y = 6 \end{cases}$

**Solution:** We will express one of the variables through the other. The easiest to express is the “y” variable from the first equation because the coefficient of y is 1:

$$y = 4 - 2x$$

Substitute in the other equation:

$$\begin{aligned} 3x - 2y &= 6 \\ 3x - 2(4 - 2x) &= 6 \\ 3x - 8 + 4x &= 6 \\ 7x - 8 &= 6 \\ 7x &= 14 \\ x &= 2 \end{aligned}$$

To find y value substitute back again:

$$\begin{aligned} y &= 4 - 2x \\ y &= 4 - 2(2) \\ y &= 0 \end{aligned}$$

The solution is the point (2, 0)

3. Solve by addition:  $\begin{cases} 4x - 5y = -7 \\ 6x + 3y = 21 \end{cases}$

**Solution:** To solve by addition we need to make the coefficient of x or y opposite numbers. If we decide to eliminate x we can multiply the first equation with 3 and the second equation with -2.

Don't forget to multiply all the terms from each equation:

$$\begin{array}{r} \begin{cases} 4x - 5y = -7 & \times 3 \\ 6x + 3y = 21 & \times -2 \end{cases} \\ + \begin{cases} 12x - 15y = -21 \\ -12x - 6y = -42 \end{cases} \\ \hline -21y = -63 \\ y = 3 \end{array}$$

To find x value substitute in one of the equations:

$$\begin{aligned} 4x - 5y &= -7 \\ 4x - 5(3) &= -7 \\ 4x - 15 &= -7 \\ 4x &= 8 \\ x &= 2 \end{aligned}$$

The solution is the point (2, 3)

4. Solve using any method:  $\begin{cases} x - 3y = 6 \\ 2x - 6y = 12 \end{cases}$

**Solution:** We can see that the second equation is divisible by 2:

$$\begin{aligned} &\begin{cases} x - 3y = 6 \\ 2x - 6y = 12 & \div 2 \end{cases} \\ &\begin{cases} x - 3y = 6 \\ x - 3y = 6 \end{cases} \end{aligned}$$

Both equations are the same:

There are infinitely many points that satisfy the system.

5. Solve using any method:  $\begin{cases} y = 5x - 1 \\ 5x - y = 3 \end{cases}$

**Solution:** The first equation is already solved for "y", so it easy to solve the system with substitution:

Substitute in the other equation:

$$\begin{aligned} 5x - (5x - 1) &= 3 \\ 5x - 5x + 1 &= 3 \\ 1 &= 3 \end{aligned}$$

This equation is never true:

No solution

6. Tickets for a show cost \$2.00 for adults and \$1.50 for children. How many adult and how many children's tickets were sold if a total of 127 tickets were sold for \$214?

**Solution:**

	How many tickets were sold:	Unit price	Price per group
Adults	$x$	\$2.00	$2x$
Children	$y$	\$1.50	$1.5y$
Total	127		214

$$\begin{cases} x + y = 127 \\ 2x + 1.5y = 214 \end{cases}$$

With substitution:

$$x = 127 - y$$

$$2(127 - y) + 1.5y = 214$$

$$254 - 2y + 1.5y = 214$$

$$-0.5y = 214 - 254$$

$$-0.5y = -40$$

$$y = 80$$

To find  $x$ :

$$x = 127 - y$$

$$x = 127 - 80$$

$$x = 47$$

There were 47 adults and 80 children

7. Recall that two angles are complementary if their sum is  $90^\circ$ . Find the measures of two complementary angles if one is 36 degrees less than the other.

**Solution:**

First angle:  $x$

Second angle:  $y$

$$\begin{cases} x + y = 90 \\ x = y - 36 \end{cases}$$

$$y - 36 + y = 90$$

$$2y = 90 + 36$$

$$2y = 126$$

$$y = 63$$

$$x = 90 - 63 = 27$$

To find the angles by substitution:

The angles are  $27^\circ$  and  $63^\circ$

8. Using function notation, write the equation of a line containing the point  $(-1, 2)$  with slope of 3.

**Solution:** Using the point-slope formula:  $y - y_1 = m(x - x_1)$

$$y - 2 = 3(x - (-1))$$

$$y - 2 = 3x + 3$$

$$y = 3x + 5$$

$$f(x) = 3x + 5$$

9. Using function notation, write the equation of a line containing the points  $(4, -1)$  and  $(-2, 5)$ .

**Solution:** The slope is:

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{5 - (-1)}{-2 - 4} = \frac{5 + 1}{-2 - 4} = \frac{6}{-6} = -1$$

Using the point-slope formula:  $y - y_1 = m(x - x_1)$

$$y - (-1) = -1(x - 4)$$

$$y + 1 = -x + 4$$

$$y = -x + 3$$

$$f(x) = -x + 3$$

10. Using function notation, write the equation of a line containing the points  $(1, -1)$  and perpendicular to  $6y + 2x = 2$ .

**Solution:** The slope of the perpendicular line is reciprocal and opposite of the slope of the line  $6y + 2x = 2$ . Solve for  $y$  this equation to find the slope:

$$6y = -2x + 2$$

$$y = \frac{-2}{6}x + \frac{2}{6}$$

$$y = \frac{-1}{3}x + \frac{1}{3}$$

The slope of the perpendicular line is  $m = -\frac{1}{3}$ . The slope of the line that is required in this problem is  $m = 3$ .

Using the point-slope formula:  $y - y_1 = m(x - x_1)$

$$y - (-1) = 3(x - 1)$$

$$y + 1 = 3x - 3$$

$$y = 3x - 4$$

$$f(x) = 3x - 4$$

11. Using function notation, write the equation of a line containing the points  $(-2, 4)$  and parallel to  $4y - 2x = 9$ .

**Solution:** The parallel lines have the same slope. Solve for  $y$  the equation  $4y - 2x = 9$  to find the slope:

$$4y - 2x = 9$$

$$4y = 2x + 9$$

$$y = \frac{2}{4}x + \frac{9}{4}$$

$$y = \frac{1}{2}x + \frac{9}{4}$$

The slope of the parallel line is  $m = \frac{1}{2}$ , so is the slope of the line that is required in this problem.

Using the point-slope formula:  $y - y_1 = m(x - x_1)$

$$y - 4 = \frac{1}{2}(x - (-2))$$

$$y - 4 = \frac{1}{2}x + 1$$

$$y = \frac{1}{2}x + 5$$

$$f(x) = \frac{1}{2}x + 5$$

12. Write the equation of the horizontal line containing the point  $(5, 3)$ . Use function notation.

**Solution:** The horizontal line has an equation  $y = b$ . In this case  $y = 3$ .

13. If  $y$  varies directly as  $x$ , find the constant of variation and the direct variation equation for this situation:  $y = 4$  when  $x = 12$ .

**Solution:** Direct variation looks like  $y = kx$ . To find  $k = ?$  we substitute the given information:

$$y = kx$$

$$4 = 12k$$

$$\frac{4}{12} = \frac{12k}{12}$$

$$k = \frac{1}{3} \Rightarrow y = \frac{1}{3}x$$

14. If  $y$  varies inversely as  $x$ , find the constant of variation and the direct variation equation for this situation:  $y = 3$  when  $x = 5$ .

**Solution:** Direct variation looks like  $y = \frac{k}{x}$ . To find  $k = ?$  we substitute the given information:

$$y = \frac{k}{x}$$

$$3 = \frac{k}{5}$$

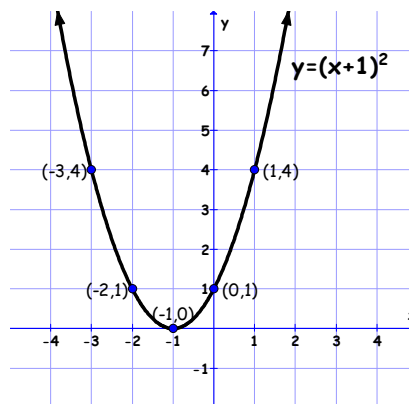
$$\frac{3}{5} = \frac{k}{5}$$

$$k = \frac{3}{5} \Rightarrow y = \frac{3}{5x}$$

15. Graph the function  $g(x) = (x+1)^2$ . Label 3 exact points. List the domain and range.

**Solution:** We always pick the first point to be the vertex of the parabola (this is the  $x$ -value that makes the expression under the square = 0. In this case this is  $x+1 = 0$ , or  $x = -1$ . Then we pick two points from each side of the vertex value and calculate the  $y$  values at them. If we work correctly the  $y$  values are going to be the same for each pair of  $x$  or the points are going to be symmetrical in respect of the axis of symmetry, which is the vertical line through the vertex:

$x$	$g(x) = (x+1)^2$
1	$(1+1)^2 = 4$
0	$(0+1)^2 = 1$
-1	$(-1+1)^2 = 0$
-2	$(-2+1)^2 = 1$
-3	$(-3+1)^2 = 4$



The vertex is at  $(-1, 0)$ .

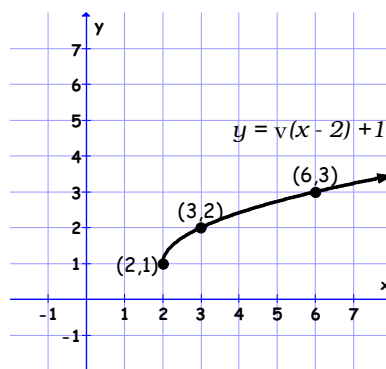
Domain:  $(-\infty, \infty)$  (because we can plug any value for  $x$ , and we see from the graph that the graph continues unlimitedly to both sides.)

Range:  $[0, \infty)$  (because there is no  $y$ -value lower than 0 on the graph; it is a closed interval, because there is a point that contains  $y=0$ .)

16. Graph the function  $f(x) = \sqrt{x-2} + 1$ . Label 3 exact points. List the domain and range.

**Solution:** We always pick the first point to be at the corner of the graph (this is the x-value that makes the expression under the square root = 0. In this case this is  $x-2 = 0$ , or  $x = 2$ . Then we pick two points from each side of the corner point and calculate the y values at them. Notice that the square root graph goes one way only so we will only receive y-values to one of the sides of this function. I picked  $x = 6$ , because it is easy to take root of 4. If I pick  $x = 4$ , or 5, then I'll have to take a root of 2 or 3, which are not exact numbers:

$x$	$f(x) = \sqrt{x-2} + 1$
0	$\sqrt{0-2} + 1 = \sqrt{-2} + 1$
1	$\sqrt{1-2} + 1 = \sqrt{-1} + 1$
2	$\sqrt{2-2} + 1 = \sqrt{0} + 1 = 1$
3	$\sqrt{3-2} + 1 = \sqrt{1} + 1 = 2$
6	$\sqrt{6-2} + 1 = \sqrt{4} + 1 = 3$



The corner point is at (2, 1).

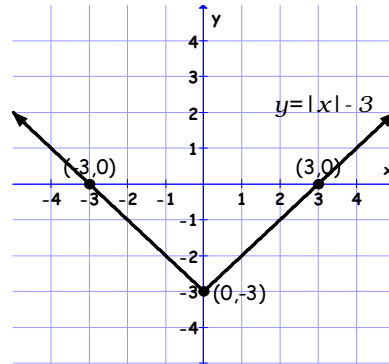
Domain:  $[2, \infty)$  (because we cannot plug values for  $x$  less than 2; if we do we get negative numbers under the root)

Range:  $[1, \infty)$  (because there is no y-value lower than 1 on the graph; it is a closed interval, because there is a point that contains  $y=1$ .)

17. Graph the function  $f(x) = |x| - 3$ . Label 3 exact points. List the domain and range.

**Solution:** We always pick the first point to be the corner point of the graph (this is the x-value that makes the expression under the absolute value = 0. In this case this is  $x = 0$ . Then we pick two points from each side of the corner point and calculate the y values at them. If we work correctly the y values are going to be the same for each pair of  $x$  or the points are going to be symmetrical in respect of the the vertical line through the corner point:

$x$	$f(x) =  x  - 3.$
2	$ 2  - 3 = 2 - 3 = -1$
1	$ 1  - 3 = 1 - 3 = -2$
0	$ 0  - 3 = 0 - 3 = -3$
-1	$ -1  - 3 = 1 - 3 = -2$
-2	$ -2  - 3 = 2 - 3 = -1$

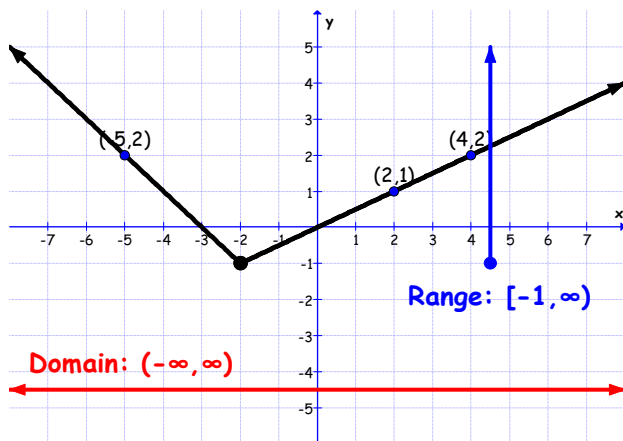


The corner is at  $(0, -3)$ .

Domain:  $(-\infty, \infty)$  (because we can plug any value for  $x$ , and we see from the graph that the graph continues unlimitedly to both sides.)

Range:  $[-3, \infty)$  (because there is no  $y$ -value lower than  $-3$  on the graph; it is a closed interval, because there is a point that contains  $y = -3$ .)

Use the graph of  $f(x)$  below to answer 18-21.



18.  $f(2) = ?$

**Solution:** The answer is the  $y$ -value of the point with  $x$  value:  $x = 2$ .  $f(2) = 1$

19. Find all values of  $x$  for which  $f(x) = 2$

**Solution:** The answer is the  $x$ -value of the point with  $y$  value:  $y = 2$ .  $x = -5$ ;  $x = 4$

20. The domain of  $f(x)$  is? **Solution:** Domain:  $(-\infty, \infty)$

21. The range of  $f(x)$  is? **Solution:** Range:  $[-1, \infty)$